# Vapor–Liquid Equilibrium in Binary and Ternary Mixtures of Nitrogen, Argon, and Methane

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Vapor-liquid equilibrium values are reported for binary and ternary mixtures of nitrogen, argon, and methane at 122.89 K. The experimental results are successfully correlated with the Peng-Robinson equation of state.

# Introduction

Vapor-liquid equilibrium (VLE) values are required in technological applications and are fundamental to separation operations. In this work we report VLE data on the three binary mixtures and the ternary system of nitrogen, argon, and methane at 122.89 K. The experimental VLE values on the binary mixtures were correlated with the Peng-Robinson equation of state, and used to predict the VLE values for the binary system. The predicted values were then compared with the experimental results. Calculated pressure and vapor composition from the equation are compared with the ternary mixture data.

Knapp (1) gives references to VLE measurements on the three binary mixtures, which contain seven sets of  $N_2 + Ar$  and  $N_2 + CH_4$  each, and five sets of  $Ar + CH_4$ . Although the temperature range of the data reported above is rather broad, and only one set of data for  $Ar + CH_4$  is at 123 K, Sprow and Prausnity (2) and Gravelle and Lu (3) reported VLE data on ternary mixtures of  $N_2$ , Ar, and  $CH_4$  at 90.67 and 123.4 K, respectively. Hence, this work may be considered as a supplement to Gravelle's work.



Figure 1. Schematic diagram of the experimental apparatus: (CH) control heater, (NC) nitrogen vaporization coil, (CT) cryostat, (PM) plug-type pressure meter, (EC) equilibrium cell, (PS) pressure sensor, (FG) feed gas, (TC) temperature controller, (LS) liquid sampling tube, (VR) volume regulator, (MP) magnetic pump, (VT) vapor sampling tube, (MT) measuring temperature meter.

| Table I.   | Experimental   | Values a   | and Calcula  | ated Deviations                               |
|------------|----------------|------------|--------------|---|
| for Nitro  | gen (1) + Argo | n (2) at 7 | T = 122.89 l | $\mathbf{K} \left( \mathbf{k}_{12} = \right)$ |
| -0.010 60) |                |            |              |   |

| experimental value         |        |            | calculated deviation |                   |  |
|----------------------------|--------|------------|----------------------|-------------------|--|
| $P/MPa$ $x_1$              |        | <b>y</b> 1 | 100[P(calc) - P]/P   | $y_1(calc) - y_1$ |  |
| 1.484                      | 0.0506 | 0.0851     | 1.16                 | -0.0007           |  |
| 1.600                      | 0.1248 | 0.1959     | 0.51                 | -0.0016           |  |
| 1.728                      | 0.2068 | 0.2975     | -0.18                | 0.0032            |  |
| 1.760                      | 0.2410 | 0.3376     | 0.75                 | 0.0037            |  |
| 1.865                      | 0.3117 | 0.4196     | 0.38                 | 0.0000            |  |
| 2.006                      | 0.3895 | 0.4945     | ~1.21                | 0.0040            |  |
| 2.008                      | 0.4079 | 0.5222     | 0.00                 | -0.0059           |  |
| 2.156                      | 0.5144 | 0.6237     | 0.09                 | -0.0104           |  |
| 2.286                      | 0.5994 | 0.7118     | -0.27                | -0.0266           |  |
| 2.453                      | 0.7092 | 0.7979     | -0.50                | -0.0248           |  |
| 2.587                      | 0.8067 | 0.8530     | 0.08                 | -0.0041           |  |
| 2.734                      | 0.8974 | 0.9214     | -0.04                | -0.0027           |  |
| 2.839                      | 0.9705 | 0.9765     | 0.57                 | -0.0004           |  |
| average absolute deviation |        |            | 0.44                 | 0.0068            |  |

Table II. Experimental Values and Calculated Deviations for Nitrogen (1) + Methane (2) at T = 122.89 K ( $k_{12} = 0.034$  99)

| experimental value         |        |            | calculated deviation |                          |  |
|----------------------------|--------|------------|----------------------|--------------------------|--|
| P/MPa x <sub>1</sub>       |        | <i>y</i> 1 | 100[P(calc) - P]/P   | $y_1(\text{calc}) - y_1$ |  |
| 0.422                      | 0.0511 | 0.4339     | -0.24                | 0.0007                   |  |
| 0.676                      | 0.1270 | 0.6524     | -0.90                | -0.0055                  |  |
| 0.867                      | 0.1923 | 0.7306     | -0.23                | -0.0017                  |  |
| 1.027                      | 0.2516 | 0.7768     | 0.10                 | -0.0023                  |  |
| 1.311                      | 0.3748 | 0.8345     | 1.70                 | -0.0027                  |  |
| 1.617                      | 0.4975 | 0.8730     | -0.81                | -0.0056                  |  |
| 1.936                      | 0.6760 | 0.9130     | 2.35                 | -0.0064                  |  |
| 1.938                      | 0.6501 | 0.9030     | -0.63                | -0.0018                  |  |
| 2.266                      | 0.7904 | 0.9369     | -0.98                | -0.0055                  |  |
| 2.580                      | 0.9121 | 0.9656     | 0.00                 | -0.0015                  |  |
| average absolute deviation |        |            | 0.80                 | 0.0034                   |  |

Table III. Experimental Values and Calculated Deviations for Argon (1) + Methane (2) at 122.89 K ( $k_{12} = 0..026$  33)

| experimental value         |                       |            | calculated deviation |                          |  |
|----------------------------|-----------------------|------------|----------------------|--------------------------|--|
| P/MPa                      | <i>x</i> <sub>1</sub> | <b>y</b> 1 | 100[P(calc) - P]/P   | $y_1(\text{calc}) - y_1$ |  |
| 0.335                      | 0.0729                | 0.3299     | -0.60                | -0.0090                  |  |
| 0.385                      | 0.1142                | 0.4238     | 0.53                 | 0.0070                   |  |
| 0.503                      | 0.2071                | 0.5976     | 0.00                 | -0.0052                  |  |
| 0.592                      | 0.2775                | 0.6777     | -0.68                | -0.0056                  |  |
| 0.708                      | 0.3799                | 0.7554     | -0.14                | -0.0012                  |  |
| 0.721                      | 0.4025                | 0.7619     | 1.69                 | 0.0069                   |  |
| 0.838                      | 0.4924                | 0.8209     | -0.36                | -0.0023                  |  |
| 0.928                      | 0.5808                | 0.8600     | 0.66                 | -0.0016                  |  |
| 1.038                      | 0.6732                | 0.8932     | -0.10                | 0.0008                   |  |
| 1.132                      | 0.7635                | 0.9267     | 0.63                 | -0.0017                  |  |
| 1.263                      | 0.8813                | 0.9634     | 1.20                 | -0.0007                  |  |
| 1.342                      | 0.9468                | 0.9843     | 1.28                 | -0.0011                  |  |
| average absolute deviation |                       |            | 0.66                 | 0.0036                   |  |

#### **Experimental Section**

A forced-recirculation apparatus is employed in this work. A schematic diagram of the apparatus is shown in Figure 1. It consists of a visual equilibrium cell, an electromagnetic

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Figure 2. Pressure P as a function of the liquid ( $\odot$ ) and vapor ( $\times$ ) mole fractions for N<sub>2</sub>(1) + Ar (2) at 122.89 K: (-) calculated from the Peng-Robinson equation, ( $\Delta$ ) liquid and vapor mole fractions from Narinskii (5) at 119.97-120.00 K.



**Figure 3.** Pressure P as a function of the liquid ( $\odot$ ) and vapor ( $\times$ ) mole fractions for N<sub>2</sub> (1) + CH<sub>4</sub> (2) at 122.89 K: (-) calculated from the Peng-Robinson equation, ( $\Delta$ ) liquid and vapor mole fractions from Stryjek et al. (6) at 122.04 K.

pump, nitrogen vaporization coils, a cryostat and its temperature control system, sampling facilities, and pressure measuring devices. In this manner, the bath temperature is regulated to within 0.2 K of the desired value, and the cell temperature is controllable to  $\pm 0.05$  K.

An electromagnetic pump is employed for recirculating the vapor through the liquid in the equilibrium cell in a closed system. The design is similar to that reported by Chang (4).

Table IV. Experimental Values and Calculated Deviations for  $N_2$  (1) + Ar(2) + CH<sub>4</sub> (3) at T = 122.89 K

|                    |                    |                       |            |            | calculated deviation    |                            |                            |
|--------------------|--------------------|-----------------------|------------|------------|-------------------------|----------------------------|----------------------------|
| experimental value |                    |                       |            | 100[P-     | <i>y</i> <sub>1</sub> . | <i>y</i> 2-                |                            |
| P/MPa              | $\boldsymbol{x_1}$ | <i>x</i> <sub>2</sub> | <b>y</b> 1 | <b>y</b> 2 | P]/P                    | (calc) -<br>y <sub>1</sub> | (cale) -<br>y <sub>2</sub> |
| 0.700              | 0.0751             | 0.1613                | 0.3761     | 0.3360     | -1.74                   | -0.0197                    | 0.0029                     |
| 0.992              | 0.2015             | 0.1081                | 0.6267     | 0.1625     | 0.31                    | 0.0012                     | -0.0043                    |
| 1.269              | 0.3147             | 0.0990                | 0.7206     | 0.1167     | 0.32                    | 0.0018                     | -0.0024                    |
| 1.289              | 0.3266             | 0.0977                | 0.7257     | 0.1120     | 0.86                    | 0.0057                     | -0.0015                    |
| 1.581              | 0.4178             | 0.1850                | 0.7185     | 0.1778     | 0.00                    | -0.0020                    | -0.0029                    |
| 1.880              | 0.5599             | 0.1513                | 0.7908     | 0.1282     | -0.70                   | -0.0015                    | -0.0002                    |
| 2.091              | 0.6408             | 0.1726                | 0.8058     | 0.1396     | -0.68                   | -0.0024                    | -0.0014                    |
| 2.235              | 0.7083             | 0.1446                | 0.8424     | 0.1129     | -0.91                   | -0.0047                    | 0.0006                     |
| 2.441              | 0.8118             | 0.1001                | 0.8939     | 0.0761     | -0.12                   | -0.0047                    | 0.0015                     |
| ε                  | verage a           | bsolute a             | leviation  | 1          | 0.63                    | 0.0050                     | 0.0020                     |
| I.                 | 6                  |                       | <u> </u>   |            |                         |                            | 1                          |



Figure 4. Pressure P as a function of the liquid ( $\odot$ ) and vapor ( $\times$ ) mole fractions for Ar (1) + CH<sub>4</sub> (2) at 122.98 K: (-) calculated from the Peng-Robinson equation, ( $\Delta$ ) liquid and vapor mole fractions from Shatkaya and Zhiruova (7) at 123.05 K.

After reaching thermal equilibrium in the cell, the vapor is recirculated within the recirculation loop, which consists of the electromagnetic pump and the equilibrium cell described above, a volume regulator, a sampling loop, and a cooling coil. When the vapor passes through the volume regulator and the sampling loop, it is heated to room temperature, but it is cooled to the bath temperature again by passing through the cooling coil inside the cryostat before returning to the equilibrium cell.

The equilibrium temperature is measured by means of a thermocouple and a potentiometer. The pressure of the system is measured by means of a pressure gauge with an accuracy of  $\pm 0.16\%$ ; the range of the gauge is 0–6 MPa.

Analyses of samples were made with a Shimadzu Model GC-9a gas chromatograph. Research grade gases supplied by the Acadomia Metrology Sinica were used without any further purification. Minimum purities of these gases are as follows: nitrogen, 99.999 mol %; argon, 99.999 mol %; methane, 99.99 mol %.

## Results

All equilibrium measurements are made at 122.89 K, and the results are presented in Tables I-IV. The binary pressurecomposition results are shown in Figures 2-4.

The VLE data are correlated with the Peng-Robinson (PR) (5) equation. Tables I-III also present the three binary interaction parameters  $k_{ij}$  of the PR equation which were obtained by applying the method of least squares through optimization on the measured binary VLE data, and the calculated deviations of the correlation from the experimental data. By using the PR equation with these  $k_{ii}$  parameters, the vapor composition and the pressure for the ternary mixtures are predicted at the experimental temperature and liquid composition. The small deviations of the predicted values from experimental data shown in Table IV reflect the consistency between the measured binary data and the

measured ternary results. The solid lines in Figures 2-4 show the calculated results by the PR equation.

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